

CHAPTER - NUMBER SYSTEM

Natural Numbers → Counting numbers are known as natural numbers. E.g. → 1, 2, 3, ... etc.

Whole Numbers → All numbers together with 0 form the collection of whole numbers.

E.g. → 0, 1, 2, 3, ... etc.

NOTE

→ Every natural no. is a whole no.

→ 0 is a whole no. but not a natural no.

Integers → All natural numbers, 0 and negatives of natural numbers form the collection of all integers.

Rational Numbers → The number of the form $\frac{p}{q}$ where p and q are integers and $q \neq 0$, are known as rational numbers.

E.g. → 1, $\frac{2}{3}$, $-\frac{3}{2}$, $\frac{5}{2}$ etc.

NOTE

→ 0 is a rational no.

→ Every natural no. is a rational no.

→ Every integer is a rational no.

Equivalent Rational Numbers
We know that,

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$$\frac{1}{2} = \frac{1 \times 2}{2 \times 2} = \frac{1 \times 3}{2 \times 3} = \frac{1 \times 4}{2 \times 4} = \frac{1 \times 5}{2 \times 5} = \dots$$

$$\Rightarrow \frac{1}{2} = \frac{2}{4} = \frac{3}{6} = \frac{4}{8} = \frac{5}{10} = \dots$$

These are known as equivalent rational numbers.

Simplest form of a Rational Number

A rational no. $\frac{p}{q}$ is said to be in simplest form, if p and q are integers having no common factor other than 1 and $q \neq 0$.

Eg. → The simplest form of each of $\frac{2}{4}$, $\frac{3}{6}$, $\frac{4}{8}$ etc is $\frac{1}{2}$.

Similarly, the simplest form of $\frac{6}{9}$ is $\frac{2}{3}$ & $\frac{95}{133}$ is $\frac{5}{7}$.

Representation of Rational Numbers on Real Line

Draw a line XY which extends endlessly in both the directions. Take a point O on it and let it represent 0 (zero).

Taking a fixed length, called unit length, mark off $OA = 1$ unit.

The midpoint B of OA denotes the rational no.

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Divide the 3rd unit BC into 8 equal parts
(as the given rational no. $2\frac{3}{8}$ has denominator 8)
from B count the 3rd part out of 8 name it P
(as the given rational no. $2\frac{3}{8}$ has numerator 3)
 \therefore P represents $2\frac{3}{8}$.

Some Important Results on Rational Numbers

(i) Let a and b be two rational no.s s.t. $x < y$.
Then,

$\frac{1}{2}(x+y)$ is a rational no. lying between x and y.

E.g. \rightarrow Find a rational no. lying between $\frac{1}{3}$ and $\frac{1}{2}$.

Solⁿ \rightarrow Let $x = \frac{1}{3}$ and $y = \frac{1}{2}$ clearly $x < y$.

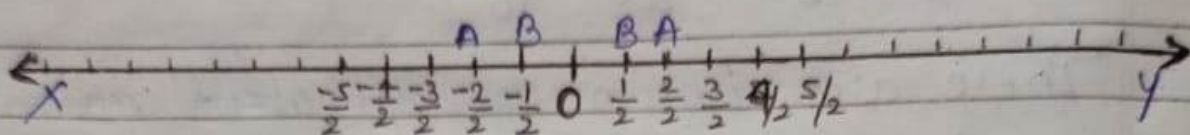
A rational no. lying between x and y
 $= \frac{1}{2}(x+y) = \frac{1}{2}\left(\frac{1}{3} + \frac{1}{2}\right) = \frac{1}{2}\left(\frac{2+3}{6}\right)$

$$= \frac{1}{2}\left(\frac{5}{6}\right)$$

$$= \frac{5}{12}$$

Hence, $\frac{5}{12}$ is a rational no. lying between $\frac{1}{3}$ and $\frac{1}{2}$.

$\frac{1}{2}$. Starting from 0, set off equal distances each equal to $OB = \frac{1}{2}$ unit.



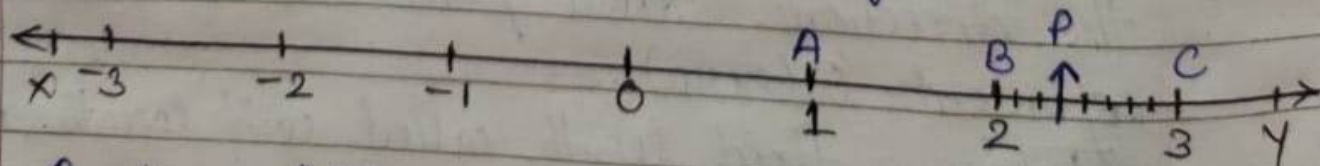
from the point 0, on its right, the points at distances equal to OB , $2OB$, $3OB$, $4OB$ etc, denote respectively the rational no. $\frac{1}{2}$, $\frac{2}{2}$, $\frac{3}{2}$, $\frac{4}{2}$ etc.

Similarly, from the point 0, on its left, the points at distances equal to OB , $2OB$, $3OB$ etc denote respectively the rational no. $-\frac{1}{2}$, $-\frac{2}{2}$, $-\frac{3}{2}$ etc.

Thus, each rational no. with 2 as denominator can be represented by some point on the number line.

E.g. \rightarrow Represent $2\frac{3}{2}$ on number line.

Solⁿ \rightarrow Draw a line XY and taking a fixed length as unit length represent integers on the line



On the right of 0, take $OA = 1$ unit, then $OB = 2$ units

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Let x and y be two rational numbers such that $x < y$.

Suppose we want to find 'n' rational nos between x and y .

$$\text{Let } d = \frac{y-x}{n+1}$$

Then, 'n' rational nos lying between x & y are -
 $(x+d), (x+2d), (x+3d), \dots, (x+nd)$

Eg. → Find five rational nos between $\frac{3}{5}$ and $\frac{4}{5}$.

Sol. → Let $x = \frac{3}{5}$ $y = \frac{4}{5}$ $n = 5$.

$$d = \frac{y-x}{n+1} = \frac{\frac{4}{5} - \frac{3}{5}}{5+1} = \frac{1}{5} \times \frac{1}{6} = \frac{1}{30}$$

Then, required rational numbers are -

$$(x+d), (x+2d), (x+3d), (x+4d) \text{ \& } (x+5d)$$

$$\text{i.e., } \left(\frac{3}{5} + \frac{1}{30}\right), \left(\frac{3}{5} + \frac{2}{30}\right), \left(\frac{3}{5} + \frac{3}{30}\right), \left(\frac{3}{5} + \frac{4}{30}\right) \text{ \& } \left(\frac{3}{5} + \frac{5}{30}\right)$$

$$\text{i.e., } \frac{19}{30}, \frac{20}{30}, \frac{21}{30}, \frac{22}{30}, \frac{23}{30}$$

$$\text{i.e., } \frac{19}{30}, \frac{2}{3}, \frac{7}{10}, \frac{11}{15}, \frac{23}{30} \text{ are the required}$$

rational numbers lying between $\frac{3}{5}$ & $\frac{4}{5}$

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Exercise

1. Write five equivalent rational numbers of -

(a) $\frac{4}{9}$

(b) $\frac{3}{2}$

(c) $-\frac{1}{3}$

(d) $-\frac{4}{5}$

(e) $2\frac{2}{3}$

(f) $-5\frac{1}{2}$

(g) $\frac{5}{7}$

(h) $\frac{1}{9}$

(i) $-\frac{2}{3}$

(j) $-\frac{3}{8}$

2. Express the following in simplest form:-

(a) $\frac{69}{92}$

(b) $\frac{473}{645}$

(c) $-\frac{1095}{1168}$

(d) $\frac{368}{496}$

(e) $\frac{148}{185}$

(f) $\frac{111}{259}$

(g) $-\frac{400}{-640}$

(h) $\frac{576}{216}$

(i) $-\frac{184}{48}$

(j) $\frac{35}{1330}$

3. Represent each of the following rational numbers on the number line -

(a) $-\frac{15}{7}$

(b) 5

(c) $-\frac{3}{7}$

(d) $\frac{5}{8}$

(e) $\frac{8}{3}$

(f) 1.3

(g) -2.4

(h) $\frac{23}{6}$

(i) $-2\frac{1}{2}$

(j) -0.5

3. Find a rational number lying between—

- | | | | |
|-------|---------------------------------|--------|-----------------------------------|
| (i) | $\frac{1}{4}$ and $\frac{1}{3}$ | (vi) | $\frac{3}{8}$ and $\frac{2}{5}$ |
| (ii) | 1.3 and 1.4 | (vii) | 0.75 and 1.2 |
| (iii) | -1 and $\frac{1}{2}$ | (viii) | $-\frac{3}{4}$ and $-\frac{2}{5}$ |
| (iv) | $\frac{3}{5}$ and $\frac{2}{3}$ | (ix) | $\frac{5}{3}$ and $\frac{1}{2}$ |
| (v) | 3 and $7\frac{1}{2}$ | (x) | -1 and -2.2 |

4. Find six rational no.s between 3 and 4.
5. Find five rational no.s between $\frac{2}{5}$ and $\frac{3}{5}$.
6. Find four rational no.s between $\frac{3}{5}$ and $\frac{2}{3}$.
7. Find nine rational numbers between 0 and 0.1.
8. Find seven rational numbers between $\frac{1}{5}$ and $\frac{1}{4}$.
9. Find five rational numbers between $\frac{2}{5}$ and $\frac{3}{4}$.
10. Find six rational numbers between $\frac{3}{7}$ and $\frac{4}{7}$.
11. Find 16 rational numbers between 2.1 and 2.2.
12. Find ten rational numbers between -1 and -2.
13. Find ten rational numbers between $2\frac{2}{3}$ and $3\frac{2}{3}$.
14. Find 16 rational numbers between 0.3 and 0.4.