

CHAPTER - INTEGERS

Various Types of Numbers

Natural Numbers → Counting numbers are called natural numbers.

Thus, 1, 2, 3, 4, ... are natural numbers.

Whole Numbers → All natural numbers together with 0 (zero) is called whole numbers.

Thus, 0, 1, 2, 3, ... are whole numbers.

Integers → All natural numbers, zero and negatives of counting numbers are called integers.

Thus, ..., -4, -3, -2, -1, 0, 1, 2, 3, ... etc are integers.

Types of Integers

(i) Positive Integer: 1, 2, 3, 4, ... etc are all positive.

(ii) Negative Integer: -1, -2, -3, etc are all negative

(iii) Zero is an integer which is neither positive nor negative.

ADDITION OF INTEGERS

Rule ① If two positive or two negative integers are added, we add their values regardless of

their signs and give the sum their common sign.

E.g. → Add: (i) 36 and 27 (ii) -31 and -25

Solⁿ: We have,

$$\begin{array}{r} \text{(i)} \quad +36 \\ \quad +27 \\ \hline \quad \quad 63 \end{array}$$

$$\begin{array}{r} \text{(ii)} \quad (-31) \\ \quad +(-25) \\ \hline \quad \quad (-56) \end{array}$$

$$\therefore 36 + 27 = \underline{63}$$

$$\therefore (-31) + (-25) = -56$$

Rule 2 To add a positive and a negative integer, we find the difference between the numerical values regardless of their sign and give the sign of the integer with the greater value to it.

E.g. → Add: (i) -47 + 18

(ii) (-29) + 52

Solⁿ → (i) $-47 + 18 = -29$

(ii) $-29 + 52 = 23$

as $\begin{array}{r} -47 \\ +18 \\ \hline -29 \end{array}$

as $\begin{array}{r} +52 \\ -29 \\ \hline +23 \end{array}$

we will put (-)ve sign
in the result as $47 > 18$

i.e. integer with the greater
value is 47 and it has

(-)ve sign.

we will put (+)ve
sign in the result

as $52 > 29$ i.e.

integer with the gre-

-ater value is 52 and

it has (+)ve sign.

Properties of Addition of Integers

① Closure property of Addition: It says that "the sum of two integers is always an integer".

- E.g. →
- $5 + 4 = 9$, $5, 4 \& 9$ all are integers.
 - $(-3) + 5 = 2$, $-3, 5 \& 2$ all are integers.

② Commutative Law of Addition: If a and b are any two integers, then

$$\boxed{a + b = b + a}$$

- E.g. →
- $(-4) + 9 = 5$ & $9 + (-4) = 5$
 - ∴ $(-4) + 9 = 9 + (-4)$

③ Associative Law of Addition: If a, b, c are any three integers, then

$$(a + b) + c = a + (b + c)$$

- E.g. →
- $\{(-6) + (-8)\} + 5 = (-14) + 5 = -9$
 - $(-6) + \{(-8) + 5\} = (-6) + (-3) = -9$
 - ∴ $\{(-6) + (-8)\} + 5 = (-6) + \{(-8) + 5\}$.

④ Existence of Additive Identity for any integer a , we have

$$a + 0 = 0 + a$$

∴ 0 is called the additive identity for integers.

E.g. → $9+0=0+9=9$
 $(-6)+0=0+(-6)=(-6)$

⑤ Existence of Additive Inverse for any integer a , we have

$$a + (-a) = (-a) + a = 0$$

The opposite of an integer a is $(-a)$

The sum of an integer and its opposite is 0.

Additive inverse of a is $(-a)$.

Similarly, additive inverse of $(-a)$ is a .

E.g. Additive inverse of 3 is -3
 Additive inverse of -5 is 5.

SUBTRACTION OF INTEGERS

for any integers a and b , we define:

(i) $a - b = a + (\text{additive inverse of } b) = a + (-b)$

(ii) $a - (-b) = a + (\text{additive inverse of } (-b)) = a + b$

<p><u>SUMMARY</u></p> $a - b = a + (-b)$ $a - (-b) = a + b$
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E.g. → Subtract : (i) 9 from 4 (ii) -9 from +5

(i)
(ii)

$$4 - 9 = 4 + (-9) = -5$$

$$5 - (-9) = 5 + 9 = 14$$

Properties of Subtraction of Integers

① Closure Property for Subtraction

If a and b are any two integers, then $(a-b)$ is always an integer.

E.g. → $2 - 5 = 2 + (-5) = -3$, $2, -5, -3$ all are integers.

② Subtraction of Integers is not Commutative

E.g. → $3 - 5 = 3 + (-5) = -2$

$$5 - 3 = 5 + (-3) = 2$$

$$\Rightarrow 3 - 5 \neq 5 - 3$$

③ Subtraction of Integers is not Associative

E.g. → $\{3 - (-4)\} - (-5) = (3 + 4) - (-5) = 7 - (-5)$
 $= 7 + 5 = 12$

$$\neq 3 - \{(-4) - (-5)\} = 3 - \{(-4) + 5\} = 3 - 1 = 2$$

$$\Rightarrow \{3 - (-4)\} - (-5) \neq 3 - \{(-4) - (-5)\}$$

Hence, subtraction of integers is neither commutative nor associative.

EXERCISE

① Evaluate:

(a) $15 + (-8)$

(b) $(-7) + (-23)$

(c) $(-32) + 47$

(d) $(-48) + (-36)$

(e) $(-16) + 9$

(f) $53 + (-26)$

② Find the sum of:

(a) $153 + (-302)$

(b) $-2035 + 297$

(c) $-489 + (-324)$

(d) $-238 + 500$

(e) $1005 + (-277)$

(f) $-1000 + 438$

③ Find the additive inverse of -

(a) -83

(b) 0

(c) 256

(d) -2001

(e) -111

(f) 32

④ Subtract:

(a) 28 from -42

(b) 318 from 0

(c) -66 from -34

(d) -56 from 144

(e) -64 from 0

(f) -37 from -53

(g) -36 from 42

(h) -153 from -240

⑤ Subtract the sum of -1032 and 136 from -34 .

6 Subtract -136 from the sum of -85 & 30. Fill in the blank:

7 (a) $\{(-13) + 27\} + (-41) = (-13) + \{27 + (\quad)\}$

(b) $(-26) + \{(-49) + (-23)\} = \{(-26) + (-49)\} + (\quad)$

(c) $53 + (-37) = (-37) + (\quad)$

(d) $(-68) + (-76) = (\quad) + (-68)$

(e) $(-72) + 0 = (\quad)$

(f) $-(-83) = (\quad)$

(g) $(-60) - (\quad) = -59$

(h) $(-31) + (\quad) = -40$

8 Simplify:

(a) $\{(-13) - (-27)\} + \{-25 + (-40)\}$

(b) $\{-26 + (-30)\} - \{-38\}$

(c) $(-68) + (-37) + (-76) - (-80)$

(d) $60 + (-30) - (-59) + (-40)$

(e) $260 + (-1000) - (-438) - 7$

9 Find $36 - (-64)$ and $(-64) - 36$. Are they equal?

10 If $a = -8$, $b = -7$, $c = 6$, verify that $(a+b) + c = a + (b+c)$

11 If $a = -9$ and $b = -6$ show: $(a-b) \neq (b-a)$

12 The sum of two integers is -16. If one of them is 53. find the other.

13 The sum of two integers is 65. If one of

them is -31 . find the other.

- (14) The difference of an integer a and (-6) is 4. Find the value of a .
- (15) Write a pair of integers whose sum gives:
- (a) zero
 - (b) a negative integer
 - (c) an integer smaller than both the integers
 - (d) an integer greater than both the integers.
 - (e) an integer smaller than only one of the integers.
 - (f) a positive integer.